

# Week 4 – Histograms, Functions

Slides by Suraj Rampure Fall 2017

#### Administrative

## 1. Project 1 comes out Friday!

Start looking for partners in this lab.

## 2. Feedback!

I'd really appreciate you giving me feedback on my teaching. Please fill out this form: **https://goo.gl/forms/YzzThyyzplmDRUKp1** sometime during lab if you haven't already.

# Histograms

An important, tricky topic! You won't get much practice with these in lab, so make sure to pay attention and read the textbook.

## What is a histogram?

A histogram is a visualization that uses rectangles to show the frequency of data points. In a histogram:

- The widths of each rectangle correspond to the intervals to which the data points belong
- The areas of each rectangle correspond to the proportion of the data that is made up by values in that interval

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#### Here's an array of some student grades.

array([79 <b>,</b>	28,	67,	41,	63,	4,	62,	50,	52,	85,	77,	69,	11,	16,	70,	32,	14,
47,	84,	23,	11,	72,	13,	82,	20,	33,	11,	24,	84,	46,	17,	56,	89,	4,
59 <b>,</b>	40,	84,	71,	10,	51,	52,	91,	14,	21,	84,	28,	12,	10,	36,	83,	27,
27,	56,	61,	39,	93,	33,	27,	95,	77,	21,	8,	10,	47,	88,	54,	40,	52,
19,	28,	77,	91,	65,	32,	90,	12,	59,	57,	52,	53,	74,	63,	15,	14,	27,
62,	55,	72,	70,	42,	25,	3,	71,	40,	78,	55,	10,	89,	56,	7]	)	

As you'll later see, to make a histogram in iPython, we need our values to be in a table. Ignore that for now.

A histogram is a visualization that uses rectangles to show the frequency of data points. In a histogram:

- The widths of each rectangle are the same, and correspond to the intervals to which the data points belong
- The areas of each rectangle correspond to the proportion of the data that is made up by values in that interval

bin	Grade count
0	5
10	9
20	11
30	9
40	13
50	12
60	15
70	6
80	12
90	8
100	0

Here, we've "binned" the original data. We now don't know exactly what the original values were, we only know the **intervals** they lie in.

bins = np.arange(0, 110, 10)

0-10, 10-20, 20-30, ... 90-100

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When defining bins, the left endpoint is included in each bin, but the right endpoint is not. For example, the counts for the value **10** are in the second bin, even the first bin was defined as **0-10**.



Simple, but powerful, formula: Area = (Height of Bar) \* (Width of Bar)



1.5% + 0.6% + 1.2% + 0.8%) = 10 \* (10%) = 100% = 1

# The **sum** of the areas of the bars in a histogram is always **1** (100%).

This is the most important fact about histograms there is. **Don't forget it!** 



Draw a histogram of the above data.





True or false (explain): The data shows that the rents are evenly distributed over the interval 250-1350.

False – Each bin contains 25% of the rents, but the bins aren't all of equal width.



What is the height and correct units of the histogram bar over the bin 350-550 on the density scale?

#### 0.125% per dollar

Since Area = Height \* Width,

Height = Area/Width = 25%/(550-350) Dollars = 0.00125 per dollar = 0.125% per dollar



#### Which bin contains more players: [2, 4) or [4, 12)?



Which bin contains more players: [2, 4) or [4, 12)?

**[4, 12)** because (2 \* 11.39) < (8 \* 3.60)

Remember, areas correspond to proportions. Larger area —> more values.



bin (million dollars)	[0,2)	[2,4)	[4,12]	[12,18)	[18,26)
height(percent per million dollars)	17.64	11.39	3.60	1.60	0.45

bin (million dollars)	[0,2)	[2,4)	[4,9)	[9,12)	[12,18)	[18,26)
height(percent per million dollars)	17.64	11.39	(i)	(ii)	1.60	0.45

The expression nba.num\_rows evaluates to 417. The expression nba.where ('salary', are.between (4,9)).num\_rows evaluates to 97.

Find the missing heights.



#### i. 97 \* 100 / (417 \* 5)

Re-arranging the area formula for height, we have that **height = area/width**. We are given that 97 out of 417 values are in the 4-9 interval, and since areas correspond to proportions, we know the area of this bar is 97/417. The width of this bar is 9 - 4 = 5. We multiply by 100 since heights in histograms are measured in percentages.



# $\frac{100 - 2(17.63) - 2(11.39) - 5\frac{97 \times 100}{417 \times 5} - 6(1.6) - 8(0.45)}{3}$

We know the total area must sum to 100%. We can then subtract the areas of all other bars from 100% to find the area of this bar. We then divide this quantity by the width of this bar to find its height.

**Functions** give us a way to write code once and use it many times. Functions in programming work similarly to the way they do in mathematics – you provide the input(s), and the function determines the output(s).



Defining a function:



value = 1432315.33
future\_value = compound\_interest(value, 0.04, 3)

#### This is fine.

```
value = 1432315.33
future_value = compound_interest(value, 0.04, 3)
multiplier
```

What about if we try to reference **multiplier**, the variable we created when defining **compound\_interest**?

**This errors!** Variables that are created inside the function definition only exist inside the function.

You can even make lists of functions, since Python treats functions as values.

functions = [max, compound\_interest, np.arange]
what\_value = functions[2](3, 10, 1)

What's the value of **what\_value**?

You can even pass in functions as parameters to other functions!

```
def combiner(f, lst):
   total = lst[0]
   for i in range(1, len(lst)):
     total = f(total, lst[i])
   return total
```

Don't worry about what this does, but notice that it calls parameter **f** as a function in the 4th line.

```
def add(a, b): return a + b
s = combiner(add, [3, 4, 12])
s
```

